## Zero-Inflated Regression Modeling for Coverage Errors of the Master Address File

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> 2014 Joint Statistical Meetings Boston, MA, USA

Disclaimer: This presentation is to inform interested parties of ongoing research and to encourage discussion of work in progress. The views expressed are those of the authors and not necessarily those of the U.S. Census Bureau.

## **Outline of Talk**

- 1. Introduction to the MAF Error Model project.
- 2. Discussion of zero-inflated count modeling in (Young and Johnson, Submitted).
- 3. Some results using an updated database.



# **MAF** Background

- The Master Address File (MAF) is an inventory of all known living quarters in the U.S. and Puerto Rico.
- A MAF extract (MAFX) is used as a frame to support several household surveys (e.g. ACS, decennial census, and ongoing demographic surveys).
- The MAF is regularly updated by operations related to the decennial census: e.g. **canvassing**, Delivery Sequence File (DSF) from U.S. Postal Service
- Two types of coverage errors:
  - 1. Undercoverage: addresses missing from the MAF
  - 2. **Overcoverage**: addresses which should be removed from the MAF
- Adds fix undercoverage and deletes fix overcoverage



# MAF Error Model (MEM) Project

- Develop statistical models for the MAF that will produce estimates of coverage errors at the census block level.
- Help characterize the quality of a particular MAFX and lend insight to frame improvement.
  - Surveys and Census operations using a MAFX could quickly estimate coverage errors at different levels of geography with the current MEM.
- Toward the goal of Targeted Address Canvassing: select an optimal set of blocks to canvass in 2019 to support 2020 Census.



# Data for MEM

Housing Units (HUs) from 2010 Census Address Canvassing (AdCan).

Blocks with > 0 HUs.

**Dependent variables**: Counts from AdCan operation:

- Adds
- Deletes

Independent variables: Candidate predictors, such as:

- American indian/hawaiian homeland indicator
- Urban/rural area
- # small, # large multi-units
- Presence of LUCA (Local Update of Census Address)
- MAF source variables
- DSF coverage variables

HU-level counts are aggregated up to block level.



#### Distributions of Adds and Deletes Updated Database

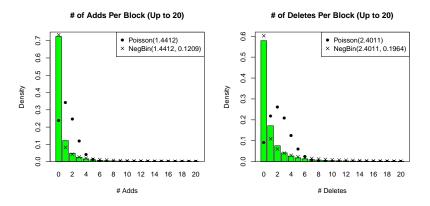


Figure: Distribution of blocks with 20 or fewer adds (left) and deletes (right).



**ZI** Regression Models for Counts

Investigated two zero-inflated (ZI) regression models for counts.

- Zero-inflated Poisson (ZIP) regression.
- Zero-inflated negative binomial (ZINB) regression.

**Regression**: To explain variability (distribution) of the observed # of adds/deletes through contributions of predictor variables.

Count model: Responses are (non-negative) counts.

- Ordinary least squares (OLS) regression is not quite appropriate.
- More granular at block level than logistic regression.

**Zero-inflation**: More zero-counts than expected under a traditional count regression model (e.g. Poisson or negative binomial).



#### Initial Variable Screening

Omitted some candidate predictor variables because they had:

- Sparse counts;
- Were collected after AdCan; or
- Caused numerical issues when included.

Looked at each non-categorical predictor variables correlation with the number of adds and deletes.

• Variables omitted if correlation coefficient < 0.05.

Resulted in 51 candidate variables for the "adds" model and 58 candidate variables for the "deletes" model.



#### Young and Johnson Methodology Collinearity

- Collinearity (i.e. high correlation) between predictors can inflate standard errors, impact numerical accuracy, and cause other issues.
- Assessed collinearity at varying thresholds of the variance inflation factor (VIF).
- Systematically omitted variables from the model at various thresholds of the VIF (i.e. 100, 25, and 10) until all remaining variables had a VIF < 10.



#### Young and Johnson Methodology Variable Selection

- Using all remaining candidate predictors, did a limited variable selection investigation to identify the "best" subset of predictors.
- Classified predictors into 6 categories.
- Used the Bayesian Information Criterion (BIC) to assess inclusion/exclusion of each set of predictors. (Smaller BIC ⇒ "better" fit).



Model Selection and Prediction Error

Using Vuong's test (Vuong, 1989), we found:

- Negative binomial fits better than Poisson.
- ZI models fits better than non-ZI models.

Prediction errors:

- Compared observed counts with counts predicted from ZI models.
- Calculated percentage of correct and incorrect predictions.
- Used 5-Fold cross-validation (CV) to check for overfitting.



Some Variables Appearing in Both Models

- Block-Level Categorical Variables: urban/rural area; American Indian/Hawaiian Homeland
- Census 2000 Variables: enumeration status not in Census; enumeration status respondent return
- **Pre-AdCan Collection Block Variables**: Basic Street Addresses that are small multi-units
- **Pre-AdCan Delivery Point Variables**: business curbline; residential curbline
- AdCan Filter Variables: Flag percentage of records valid for AdCan delivery
- All Other Variables: percentage of seasonal records; percentage of vacant records

For ZINB: Out of 307 candidate predictors, 39 used in "adds" model and 38 used in "deletes" model.

#### Informing Address Canvassing

- Good predictions can identify regions with many potential adds and/or deletes.
- Using the models, we can estimate coverage errors vs. canvassing effort (e.g. % of blocks canvassed).
- Receiver operating characteristic (ROC) curve:
  - ► True Positive Rate (TPR): # blocks that need for canvassing that need it # blocks that need canvassing.
  - ► False Positive Rate (FPR): # blocks marked for canvassing that don't need it # blocks that don't need canvassing
- A limitation is the version of the data used to fit models. The further removed we are from the 2010 AdCan operation, the more difficult it becomes to accurately quantify block-level adds/deletes.



# Results from Updated Database

#### Refitting the Adds Model

- Data contains 6,585,686 blocks with 144,617,812 HUs.
- 873 available predictors: One binary, one categorical (4 levels), rest are proportions.
- Removed 155 proportions which were constant over all blocks.
- Kept 167 of proportion variables, having |corr| > 0.01 to adds.
- After VIF analysis, kept 55 variables.
- Dropped variables with low significance (p-value > 0.01) in ZINB and ZIP models.
- Obtained models:
  - ► ZINB: 52 variables in NegBin regression, 1 (categorical) in ZI regression.
  - ZIP: 53 variables in Poisson regression, 2 (categorical + binary) in ZI regression.

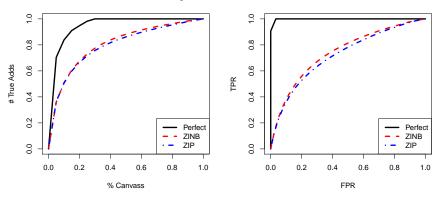


#### **Results from Updated Database**

Quality of Canvassing using Predictions and ROC



**ROC Curves** 





#### Results from Updated Database Coverage Estimates

• Consider the following measure of MAF Undercoverage error

$$\mathsf{Undercoverage} = \frac{\mathsf{Total} \ \# \ \mathsf{Adds}}{\mathsf{Total} \ \# \ \mathsf{HUs}},$$

	Actual	ZINB	ZIP
Undercoverage	0.066	0.085	0.054

- These quantities are simply for our assessment and are not based on any previous Census methodology, such as that in (Mule, 2008).
- "Actual" is computed from the database. It is not referencing published numbers and is used solely for comparison with models.



#### Some Next Steps

Investigate new variables being added to database.

• Title 26 data, AdRecs, ...

Want flexibility to update models with new data sources.

• Spatial data, economic indicators, ...

Develop an approach for determining adds in zero-blocks.

• E.g. use distance measures between blocks with larger number of adds and the zero-blocks

Bivariate regression models for adds and deletes

• Diagonal inflation?



## References

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#### **Contact Information**

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#### Thank you!

